



MAX CoE/ENCCS Workshop on efficient materials modelling on HPC with Quantum ESPRESSO, Siesta, and Yambo

## Hands-on session – Day 2 TDDFPT FOR HPC AND GPUs

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NATIONAL CENTRE OF COMPETENCE IN RESEARCH

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## Ab initio spectroscopy

#### Time-Dependent Density-Functional Perturbation Theory (TDDFpT)



### Charge Fluctuations Time-Dependent Density-Functional Perturbation Theory

Kohn-Sham  
hamiltonian  
$$(\hat{H}^{\circ} - \epsilon_{n,\mathbf{k}}^{\circ} - \hbar\omega)|\psi_{n,\mathbf{k}+\mathbf{q}}^{\prime}(\omega)\rangle = -\hat{P}_{\mathcal{C}}\left[\hat{V}_{\mathrm{Hxc},\mathbf{q}}^{\prime}(\omega) + \hat{V}_{\mathrm{ext},\mathbf{q}}^{\prime}(\omega)\right]|\psi_{n,\mathbf{k}}^{\circ}\rangle$$

$$(\hat{H}^{\circ} - \epsilon_{n,-\mathbf{k}}^{\circ} + \hbar\omega)|\psi_{n,-\mathbf{k}-\mathbf{q}}^{\prime*}(-\omega)\rangle = -\hat{P}_{\mathcal{C}}\left[\hat{V}_{\mathrm{Hxc},\mathbf{q}}^{\prime}(\omega) + \hat{V}_{\mathrm{ext},\mathbf{q}}^{\prime}(\omega)\right]|\psi_{n,-\mathbf{k}}^{\circ*}\rangle$$

$$(2 \text{ X nbnd X nks})$$

$$(2 \text{ coupled equations})$$

$$(2 \text{ Nond X nks})$$

$$(2 \text{ Nond X$$

• Invert the linear system **for each frequency** to build the response density matrix

$$\hat{
ho}'_{f q}(\omega) = \sum_{n,{f k}}^{
m occ.} \left[ |\psi_{n,{f k}+{f q}}'(\omega)
angle \langle \psi_{n,{f k}}^{\circ}| + |\psi_{n,-{f k}-{f q}}'(-\omega)
angle \langle \psi_{n,-{f k}}^{\circ*}| 
ight]$$

• Compute the dynamical susceptibility

$$n'(\mathbf{q},\omega) = \chi(\mathbf{q},\mathbf{q},\omega) V'_{\mathrm{ext},\mathbf{q}}(\omega) = \mathrm{Tr}\Big[\hat{n}^{\dagger}_{\mathbf{q}}\hat{
ho}'_{\mathbf{q}}(\omega)\Big]$$
  
  $\propto$  EELS cross section

Cost of static linear response X number of frequencies

### Charge Fluctuations Time-Dependent Density-Functional Perturbation Theory



#### **Option 2: Lanczos approach**

- Recast as a unique linear problem  $\left(\hbar\omega \mathcal{L}_{\mathbf{q}}(\omega)\right) \cdot \hat{
  ho}'_{\mathbf{q}}(\omega) = \left[\hat{V}'_{\mathrm{ext},\mathbf{q}}(\omega), \hat{
  ho}^{\circ}
  ight]$
- The response density matrix can be represented as an array of response orbitals ('batch').
- The action of the Liouvillian on the batch costs roughly twice a static linear response step.

# Charge Fluctuations Time-Dependent Density-Functional Perturbation Theory

**Option 2: Lanczos approach** 

$$\left( \hbar \omega - \mathcal{L}_{\mathbf{q}}(\omega) 
ight) \cdot \hat{
ho}'_{\mathbf{q}}(\omega) = \left[ \hat{V}'_{ ext{ext},\mathbf{q}}(\omega) \,, \hat{
ho}^{\circ} 
ight]$$

For adiabatic xc kernels

• Tridiagonalize the Liouvillian via Lanczos recursion (computationally intensive part).

### HPC implementation EXERCISE: TURBO\_EELS.X

The turbo\_eels workflow for modes at a single q point



### HPC implementation EXERCISE: EELS IN BULK SILICON

Go to the directory with the input files:

#### cd Day-2/exercise\_eels

In this directory you will find:

- \* README.md File describing how to do the exercise
- % pw.Si.scf.in Input file for the SCF ground-state calculation
- \* turbo\_eels.Si.tddfpt.in Input file for the EELS calculation
- \* turbo spectrum.Si.pp.in-Input file for post processing calculation
- \* reference Directory with the reference results

## The eels workflow PWSCF SIMULATION, STEP 1

#### 1. cd Day-2/exercise-eels

Perform a self-consistent field ground-state calculation for silicon using the *pw*.x program.

- Open and check pw.Si.scf.in
- Open and check submit\_pw.slurm
- Submit the job file

```
&control
   calculation = 'scf'
   restart_mode = 'from_scratch'
  prefix
               = 'Si'
  pseudo_dir = '../../pseudo'
  <u>out</u>dir
               = './tempdir'
  verbositv
               = 'high'
&system
  ibrav
            = 2
  celldm(1) = 10.26
  nat
            = 2
  ntyp
            = 1
  ecutwfc = 20.0
&electrons
   conv thr = 1.0d-10
ATOMIC_SPECIES
Si 28.08 Si.upf
ATOMIC_POSITIONS alat
Si 0.00 0.00 0.00
Si 0.25 0.25 0.25
K_POINTS automatic
12 12 12 0 0 0
```

## The eels workflow EELS CALCULATION, STEP 2

#### 2. cd Day-2/exercise-eels

Perform a Lanczos coefficients calculation using the turbo\_eels.x program.

- Open and check turbo\_eels.Si.tddfpt.in



- Submit the job file submit\_eels.slurm

### The eels workflow **SPECTRUM CALCULATION, STEP 3**

11

10.5

10

Even iterations Odd iterations



Perform spectrum using the turbo\_spectrum.x program.

Open and check turbo\_spectrum.Si.pp.in



Submit the job file submit\_spectrum.slurm

## turbo\_eels.x IMPLEMENTED FEATURES

- $\checkmark$  Metals and insulators
- ! Non-magnetic systems only
- Spin-orbit coupling (fully relativistic approach)
- ✓ LDA, GGA functionals (+U, work in progress)
- ✓ Norm-conserving and ultrasoft pseudopotentials
- ✓ Use of symmetries to reduce k-points (nks)
- ✓ R&G, k-point parallelization
- ✓ GPU offloading (new!)

### Spin Fluctuations Time-Dependent Density-Functional Perturbation Theory

Kohn-Sham  
hamiltonian  
$$(\hat{H}^{\circ} - \epsilon_{n,\mathbf{k}}^{\circ} - \hbar\omega)|\psi_{n,\mathbf{k}+\mathbf{q}}'(\omega)\rangle = -\hat{P}_{\mathcal{C}}\left[\hat{V}'_{\mathrm{Hxc},\mathbf{q}}(\omega) + \hat{V}'_{\mathrm{ext},\mathbf{q}}(\omega)\right]|\psi_{n,\mathbf{k}}^{\circ}\rangle$$
$$(\hat{H}^{\circ} - \epsilon_{n,-\mathbf{k}}^{\circ} + \hbar\omega)\hat{T}|\psi_{n,-\mathbf{k}-\mathbf{q}}'(-\omega)\rangle = -\hat{P}_{\mathcal{C}}^{+}\left[\hat{V}'_{\mathrm{Hxc},\mathbf{q}}(\omega) + \hat{V}'_{\mathrm{ext},\mathbf{q}}(\omega)\right]\hat{T}|\psi_{n,-\mathbf{k}}^{\circ}\rangle$$
$$\mathsf{Time-reversal operator}$$
$$\hat{O}_{\mathbf{q}}^{+}(\omega) = \hat{T}\hat{O}_{-\mathbf{q}}(-\omega)\hat{T}^{-1}$$
Resonant and anti-resonant response of the (n,k) state

- Recast as a unique linear problem  $\left(\hbar\omega \mathcal{L}_{\mathbf{q}}(\omega)\right) \cdot \hat{
  ho}'_{\mathbf{q}}(\omega) = \left[\hat{V}'_{\mathrm{ext},\mathbf{q}}(\omega), \hat{
  ho}^{\circ}
  ight]$
- The response density matrix can be represented as an array of response orbitals ('batch').

$$\hat{\rho}_{\mathbf{q}}^{\prime}(\omega) \rightarrow \begin{pmatrix} \psi_{n,\mathbf{k}+\mathbf{q}}^{\prime}(\omega) \\ \hat{T}\psi_{n,-\mathbf{k}-\mathbf{q}}^{\prime}(-\omega) \end{pmatrix}_{n,\mathbf{k}}$$

batch size = 4 x npw x nbnd x nks) complex numbers

• The action of the Liouvillian on the batch costs roughly twice a static linear response step.

### Spin Fluctuations Time-Dependent Density-Functional Perturbation Theory

Lanczos approach

$$\hbar \omega - \mathcal{L}_{f q}(\omega) \Big) \cdot \hat{
ho}'_{f q}(\omega) = \left[ \hat{V}'_{ ext{ext},f q}(\omega), \hat{
ho}^{\circ} 
ight] \, .$$

For adiabatic xc kernels

• Tridiagonalize the Liouvillian via Lanczos recursion (computational intensive part).

## HPC implementation EXERCISE: TURBO\_MAGNON.X



### HPC implementation EXERCISE: MAGNONS IN BULK IRON

Go to the directory with the input files:

#### cd Day-2/exercise\_magnor

In this directory you will find:

- \* README.md File describing how to do the exercise
- % pw.Fe.scf.in Input file for the SCF ground-state calculation
- \* turbo magnon.Fe.tddfpt.in Input file for the magnon calculation
- % turbo\_spectrum.Fe.pp.in-Input file for post processing calculation
- \* reference Directory with the reference results

## The magnon workflow PWSCF SIMULATION, STEP 1

#### 1. cd Day-2/exercise-magnon

Perform a self-consistent field ground-state calculation for iron using the pw.x program.

- Open and check pw.Fe.scf.in
- Open and check submit\_pw.slurm
- Submit the job file

&control	
calculatio	n = 'scf'
restart_mo	de = 'from_scratch'
prefix	= 'Fe'
outdir	= './tempdir'
pseudo_dir	= '//pseudo'
verbosity	= 'high'
/	
&system	
nosym	= .true.
noinv	= .true.
noncolin	= .true.
lspinorb	= .false.
ibrav	= 3
celldm(1)	= 5.406
nat	= 1
ntyp	= 1
ecutwfc	= 40
occupation	s = 'smearing'
smearing	= 'gaussian'
degauss	= 0.01
starting_m	agnetization(1) = 0.15
/	
&electrons	
<pre>mixing_bet</pre>	a = 0.3
conv_thr	= 1.d-12
/	
ATOMIC_SPECIES	
Fe 55.85 Fe	.pz-n-nc.UPF
ATOMIC_POSITIONS alat	
Fe 0.00000000 0.0000000 0.0000000	
K_POINTS automatic	
4 4 4 0 0 0	

## The magnon workflow MAGNON CALCULATION, STEP 2

2. cd Day-2/exercise-magnon

Perform a Lanczos coefficients calculation using the turbo\_magnon.x program.

- Open and check turbo\_magnon.Fe.tddfpt.in



Submit the job file submit\_magnon.slurm

## The magnon workflow SPECTRUM CALCULATION, STEP 3

3. cd Day-2/exercise-magnon

Perform spectrum using the turbo\_spectrum.x program.

- Open and check turbo\_spectrum.Fe.pp.in



- Submit the job file submit\_spectrum.slurm
- grep chi\_2\_2 Femag.plot\_chi.dat &> Chi\_2\_2.dat & and use the script for gnuplot

## turbo\_magnon.x IMPLEMENTED FEATURES

- $\checkmark$  Metals and insulators
- Spin-orbit coupling (fully relativistic approach)
- ✓ LDA functionals (+U, work in progress)
- ✓ Norm-conserving pseudopotentials only
- ! No symmetry is used (set noinv = .true. and nosym = .true. in the pw input)
- ✓ R&G, k-point parallelization
- ✓ GPU offloading (new, work in progress)