

# Converging calculations

Mesh, k-points and SCF convergence: hands on  
Catalina Coll

13th March 2023



# Quality/accuracy/precision

Time (CET)	Topic
09:00-09:45	SIESTA basics
09:45-10:30	A first contact with SIESTA: inputs, execution and outputs
10:30-10:45	Break
10:45-11:30	Basis sets
11:30-12.00	Basis set optimization
12:00-13:00	Convergence (K points, Mesh, Mixing)

## Tutorials

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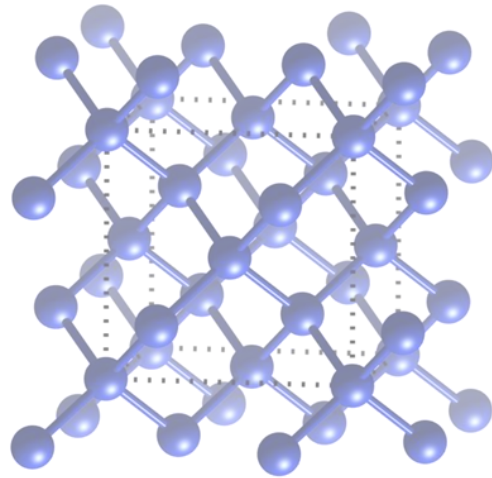
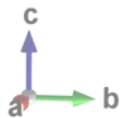
```
cp /leonardo_work/EUHPC_TD02_030/siesta-tutorials/day3-wed/04* ./
```

# Sampling

# Sampling

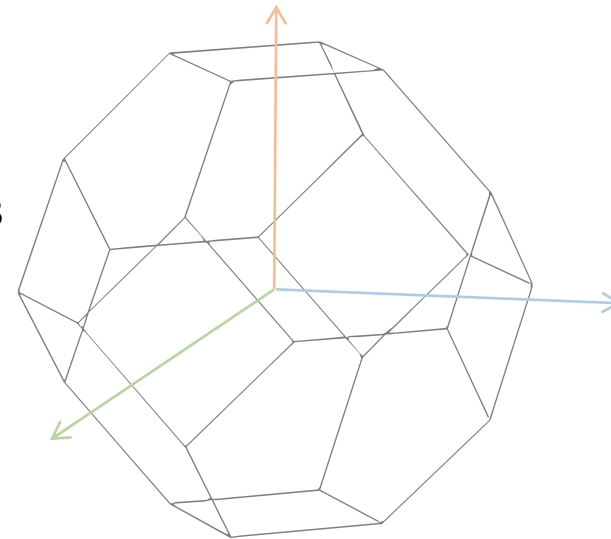
## Real space

- Potentials
- Densities
- Basis

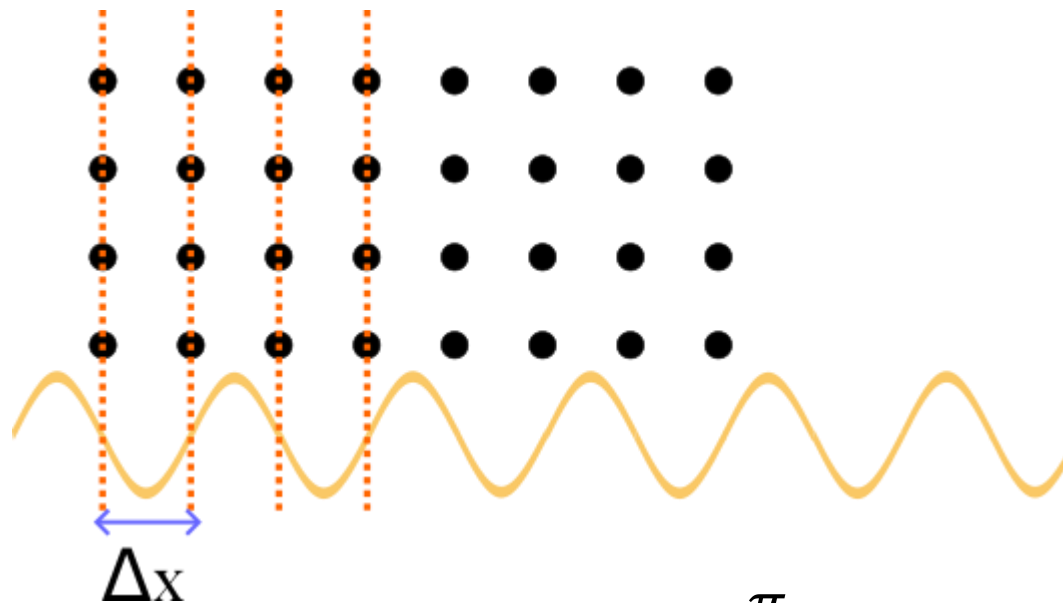
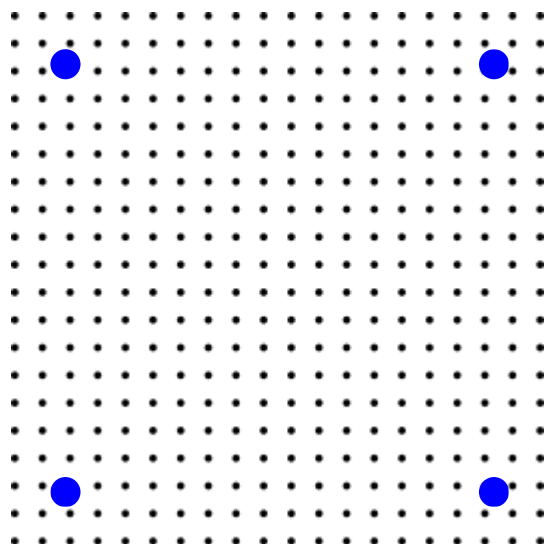


## Reciprocal space

- Density of states
- Bandstructure



# Real space grid



$$\Delta x \rightarrow k_c = \frac{\pi}{\Delta x} \rightarrow E_c = \frac{\hbar^2 k_c^2}{2m_e}$$

Fineness  $\leftrightarrow$  Maxim energy avoiding aliasing

$$\Delta x \leftrightarrow E_c \quad \text{MeshCutoff}$$

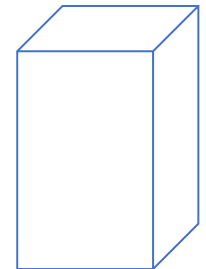
Energy units (Ry)

# Real space grid: MeshCutoff

- What is it set by the user?
  - Mesh.Cutoff 300 Ry (default)
- What is set by siesta?
  - MESH =  $18 \times 18 \times 30 = 9720$
  - Mesh cutoff (required, used) = 100.000 101.039 Ry
- How can one decide the good value?
  - Minimize the total energy.
  - Total force to zero.
  - Reasonable time (relatively small systems)

```
Mesh.Cutoff 100 Ry
```

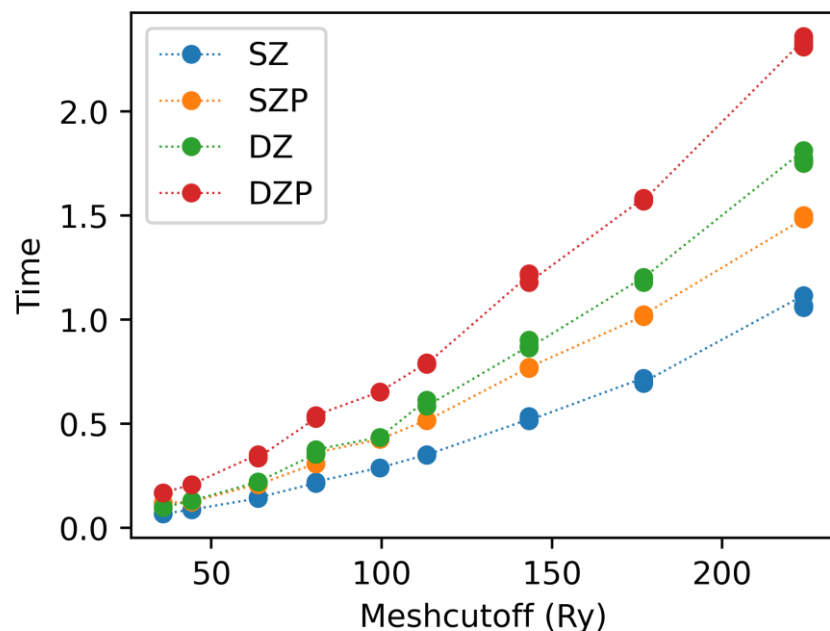
Input structure  $\longrightarrow$  Lattice vectors



# Real space grid: MeshCutoff

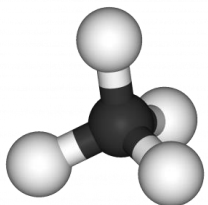
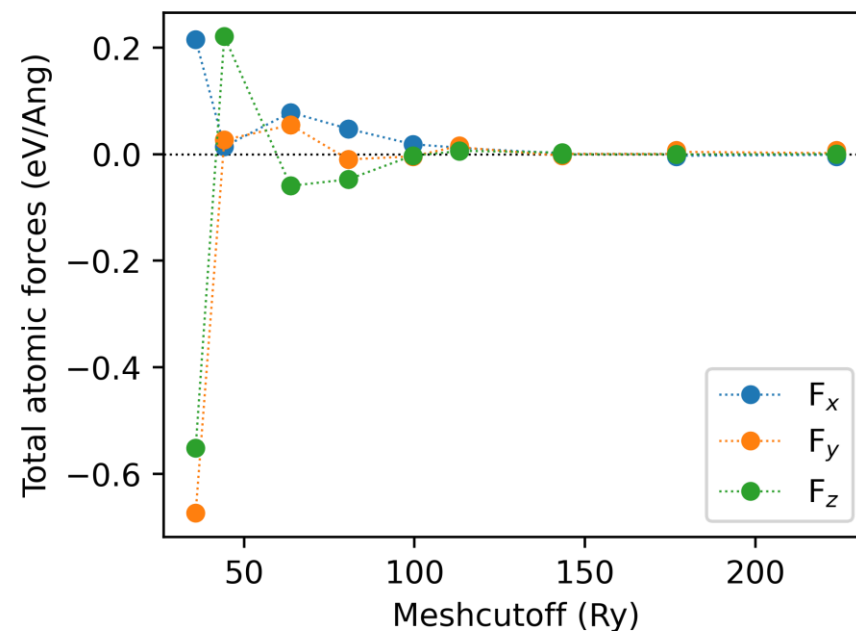
Time

TIMES file



Force

siesta: Atomic forces (eV/Ang):

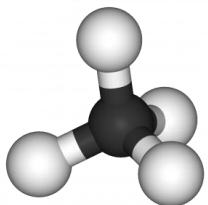
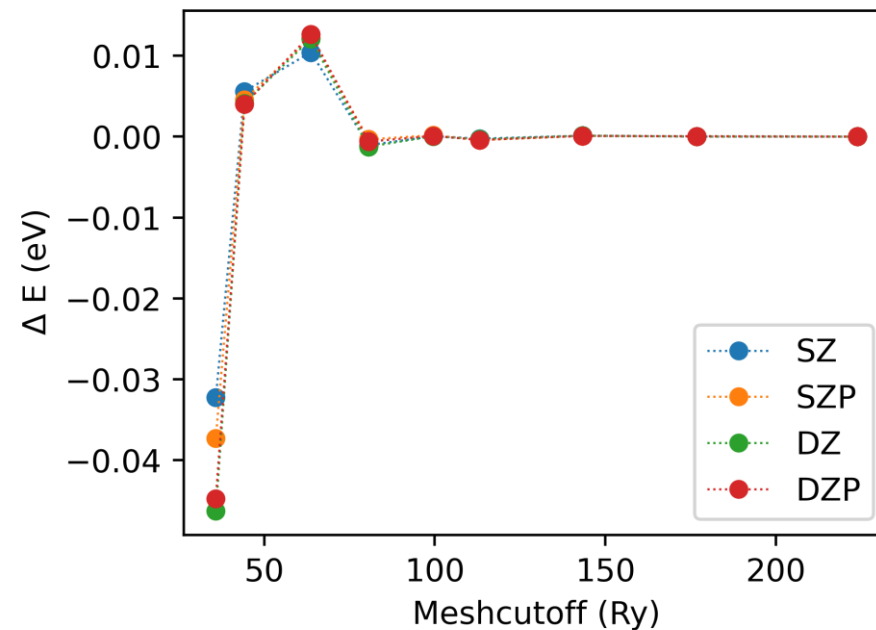
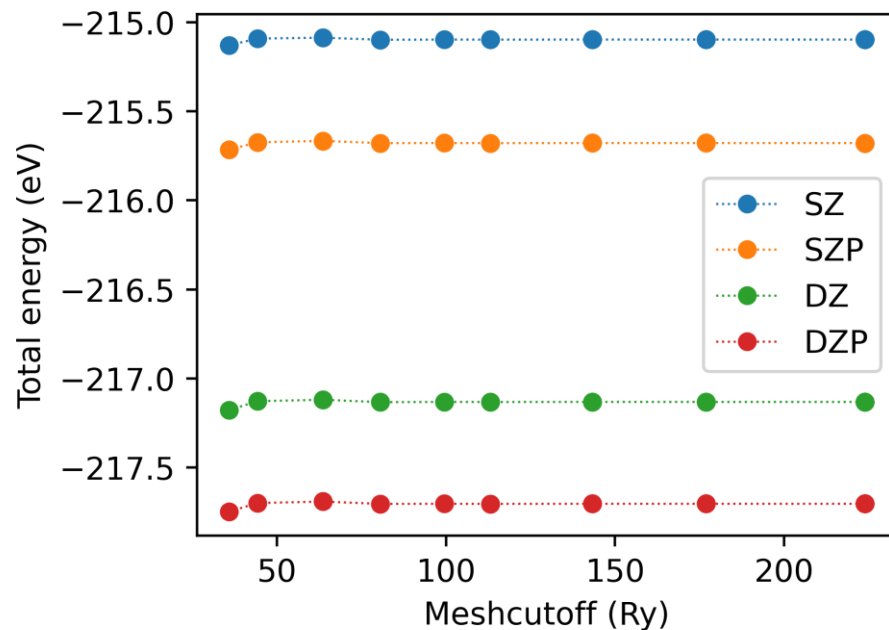


Results for methane (CH<sub>4</sub>)

# Real space grid: MeshCutoff

Energy

```
siesta: Final energy (eV):
```



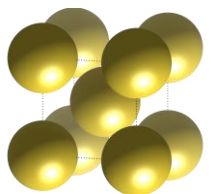
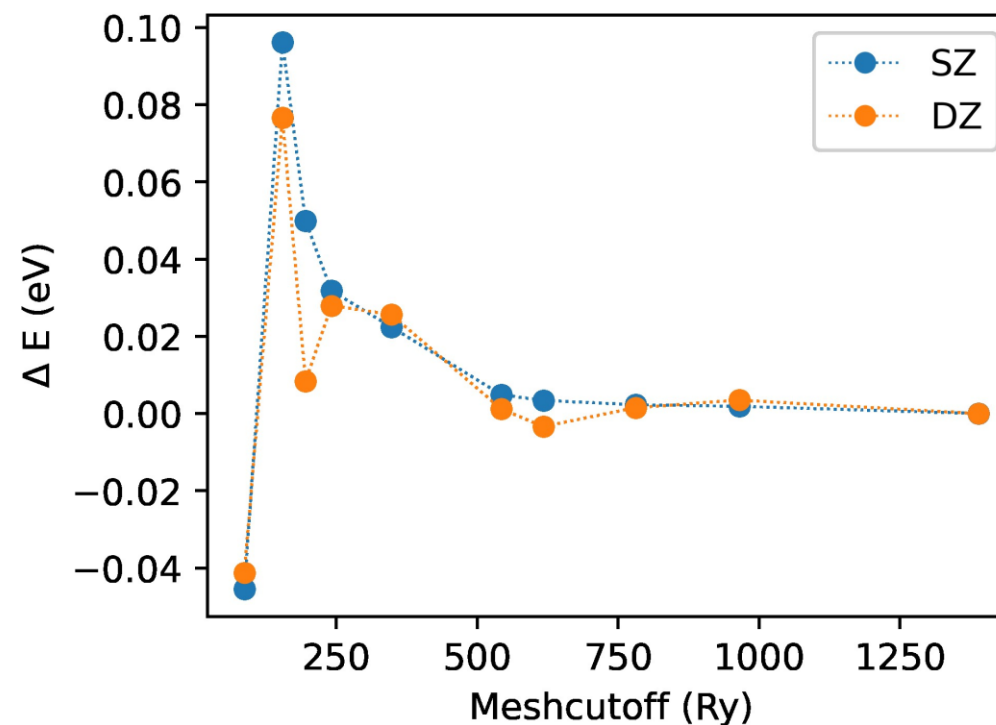
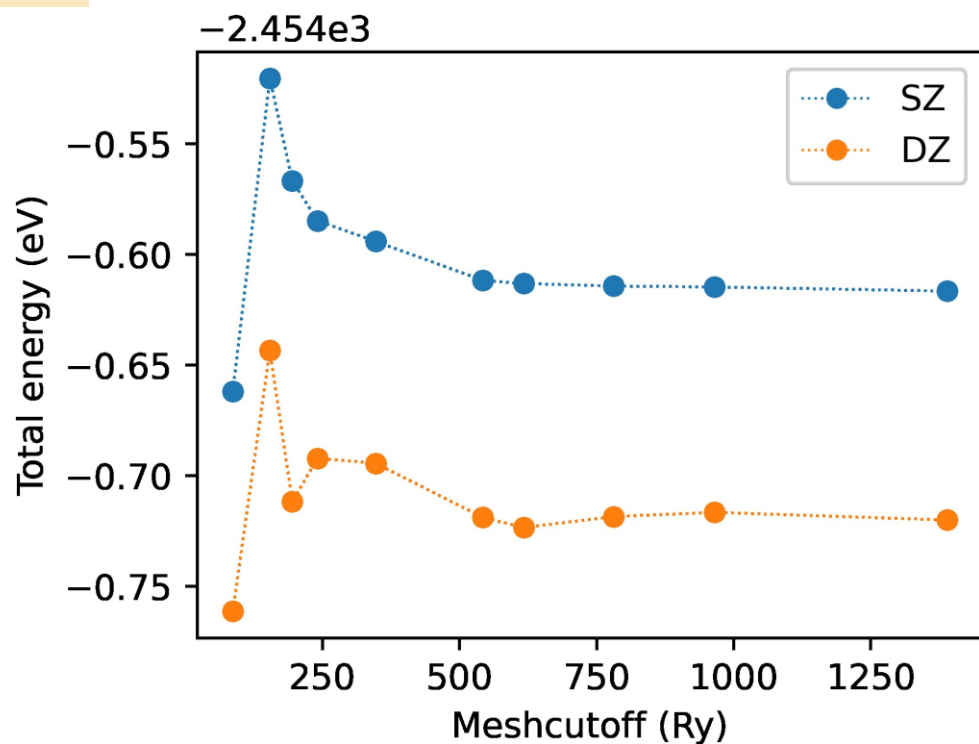
Results for methane (CH<sub>4</sub>)



# Real space grid: MeshCutoff

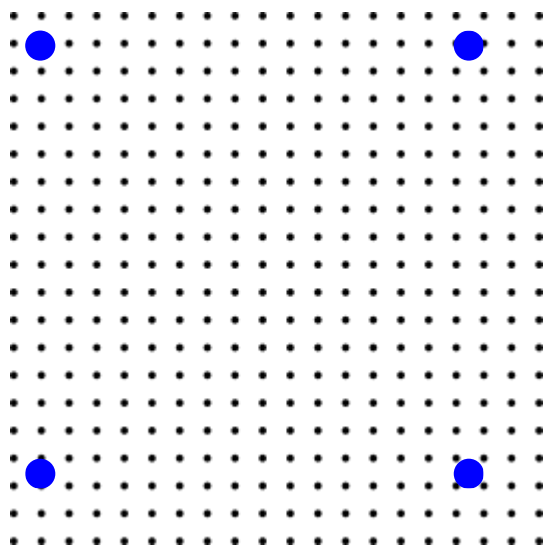
## Energy

siesta: Final energy (eV):



Results for sodium (Na)

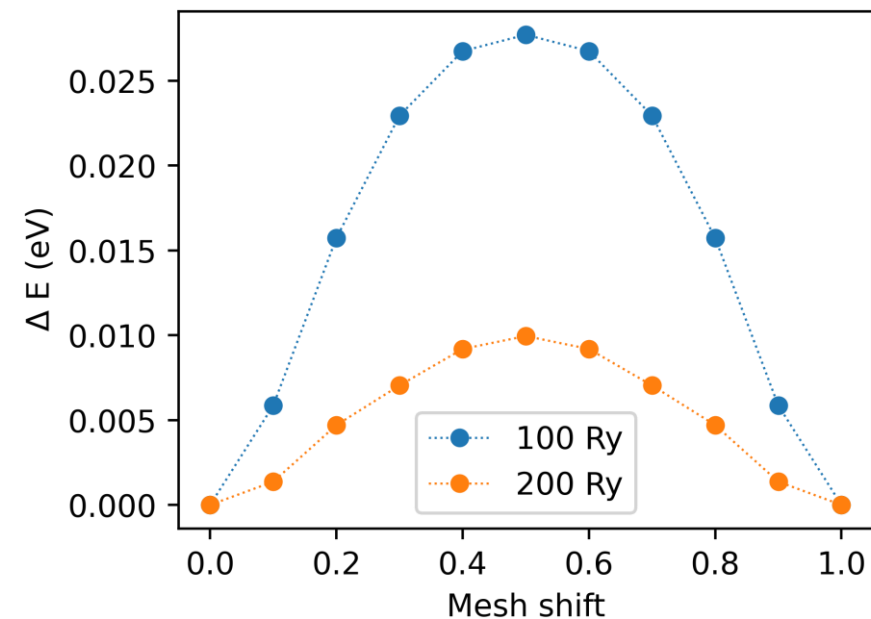
# Egg-box effect



Invariant under any translation?

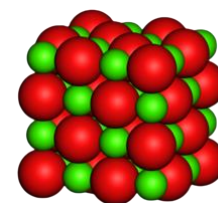
```
%block AtomicCoordinatesOrigin
0.0 0.0 0.0
%endblock AtomicCoordinatesOrigin
```

$$\delta z_{shift} = \left(\frac{1}{M_z}\right) \frac{1}{10}$$



Solutions:

- Increase Meshcutoff
- Use “grid-cell-sampling”



Results for magnesium oxide (MgO)

# Let's try it

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**Day3-wed/04a-GridConvergence**

# Reciprocal space grid

Crystals

$\psi(\mathbf{r})$

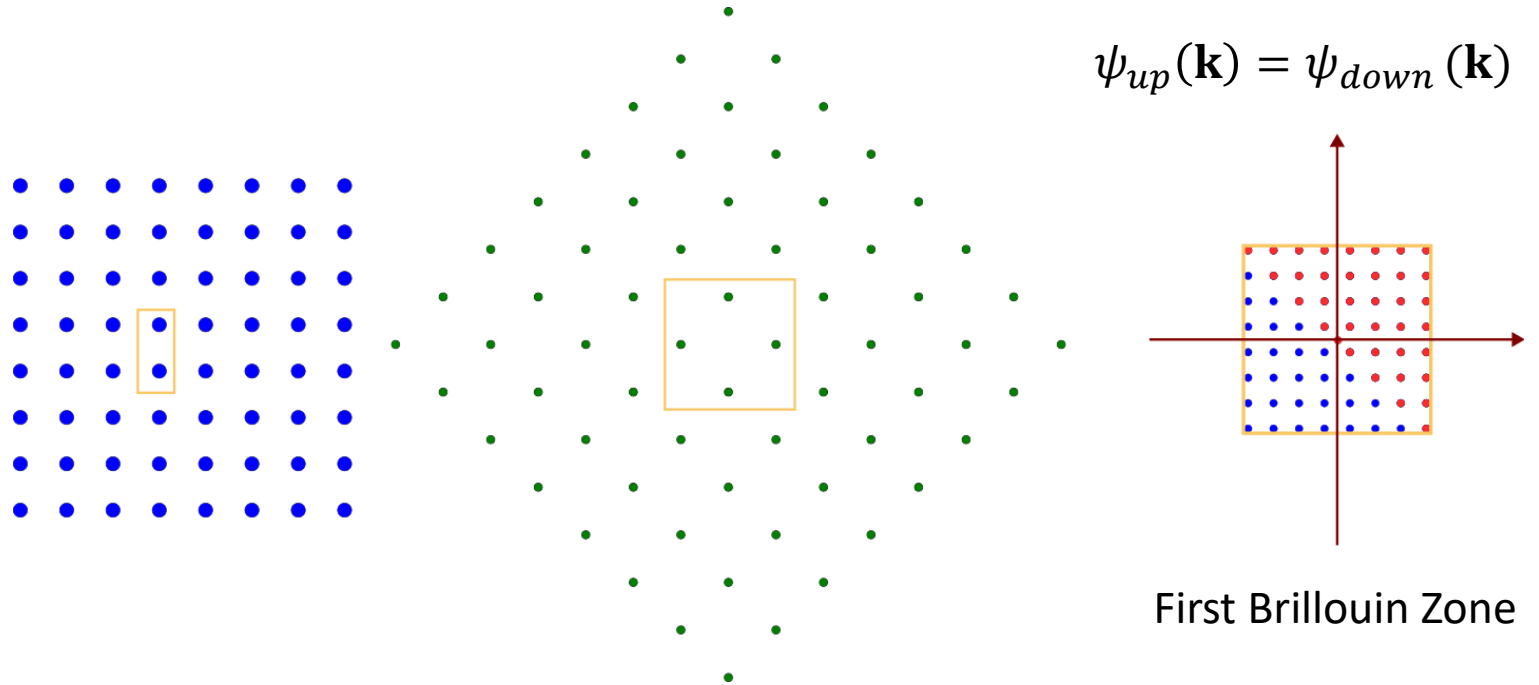
Infinite matrix

Periodicity

Reciprocal space

$$\psi_{n,\mathbf{k}+\mathbf{G}}(\mathbf{r}) = \psi_{n,\mathbf{k}}(\mathbf{r})$$

Finite matrix



# Reciprocal space grid: k-mesh

- What is it set by the user?
  - k grid cut off
  - Monkhorst Pack grid
- What is set by siesta?
  - SystemLabel.KP
- How can one decide the good value?
  - Must consider the ratio between the lattice vectors.
  - Check: Energy
    - DOS
    - Bandstructure
  - For metallic systems more k points will be needed.

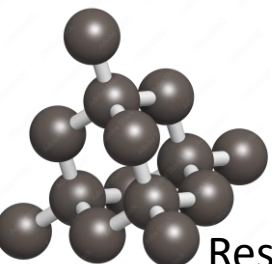
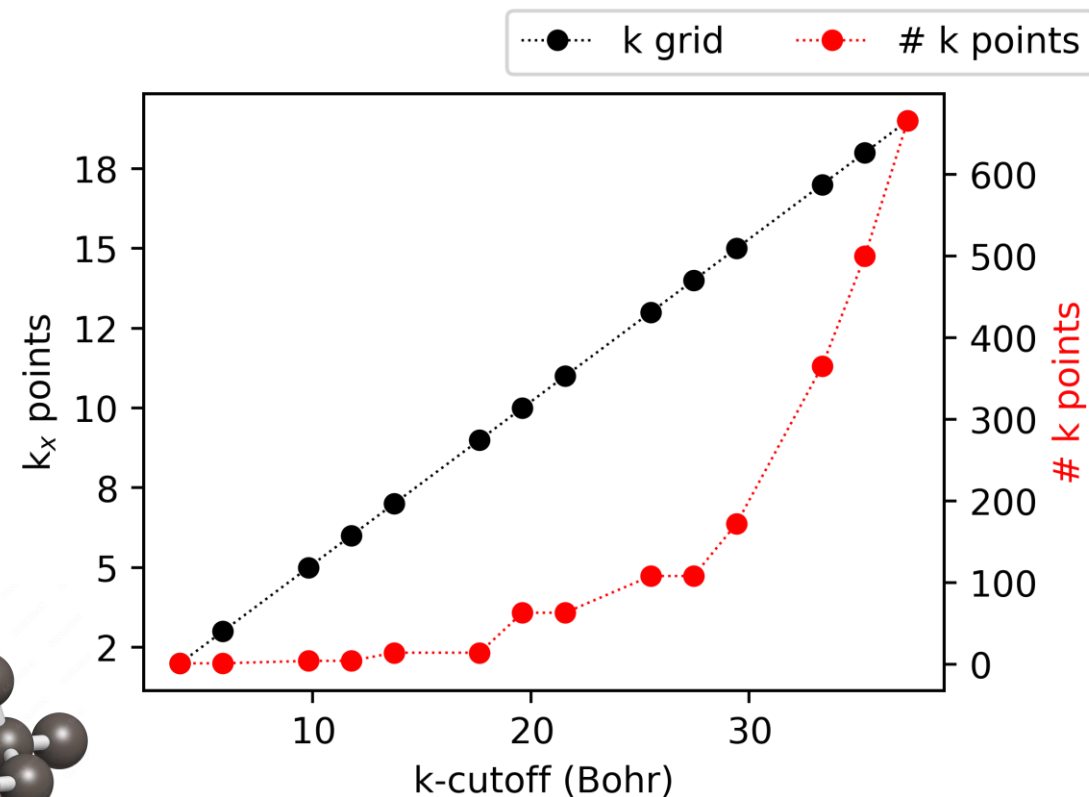
Input structure → Lattice vectors



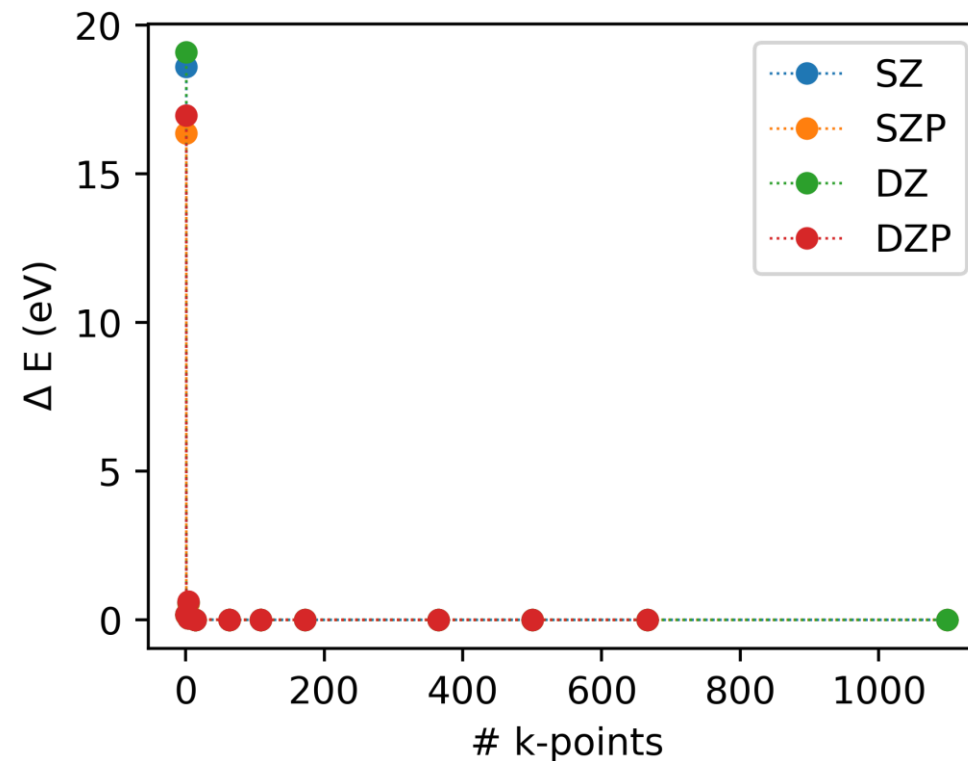
```
kgrid_cutoff 10.0 Ang
%block kgrid Monkhorst_Pack
  6 0 0 0.0
  0 6 0 0.0
  0 0 1 0.0
%endblock kgrid_Monkhorst_Pack
```

	Coordinates (Bohr <sup>-1</sup> )			Weight
SystemLabel.KP	22			
1	-0.447497E+00	-0.258363E+00	0.000000E+00	0.555556E-01
2	-0.223749E+00	-0.129181E+00	0.000000E+00	0.555556E-01
3	0.000000E+00	0.000000E+00	0.000000E+00	0.277778E-01
4	0.671246E+00	0.387544E+00	0.000000E+00	0.277778E-01
5	-0.447497E+00	0.111022E-15	0.000000E+00	0.555556E-01
6	-0.223749E+00	0.129181E+00	0.000000E+00	0.555556E-01
7	0.000000E+00	0.258363E+00	0.000000E+00	0.555556E-01
8	0.223749E+00	0.387544E+00	0.000000E+00	0.555556E-01
9	0.447497E+00	0.516726E+00	0.000000E+00	0.555556E-01
10	0.671246E+00	0.645907E+00	0.000000E+00	0.555556E-01
11	-0.447497E+00	0.258363E+00	0.000000E+00	0.555556E-01
12	-0.223749E+00	0.387544E+00	0.000000E+00	0.555556E-01
13	0.000000E+00	0.516726E+00	0.000000E+00	0.555556E-01
14	0.223749E+00	0.645907E+00	0.000000E+00	0.555556E-01
15	0.447497E+00	0.775088E+00	0.000000E+00	0.555556E-01
16	0.671246E+00	0.904270E+00	0.000000E+00	0.555556E-01
17	-0.447497E+00	0.516726E+00	0.000000E+00	0.277778E-01
18	-0.223749E+00	0.645907E+00	0.000000E+00	0.277778E-01
19	0.000000E+00	0.775088E+00	0.000000E+00	0.277778E-01
20	0.223749E+00	0.904270E+00	0.000000E+00	0.277778E-01
21	0.447497E+00	0.103345E+01	0.000000E+00	0.277778E-01
22	0.671246E+00	0.116263E+01	0.000000E+00	0.277778E-01

# k sampling

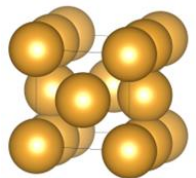
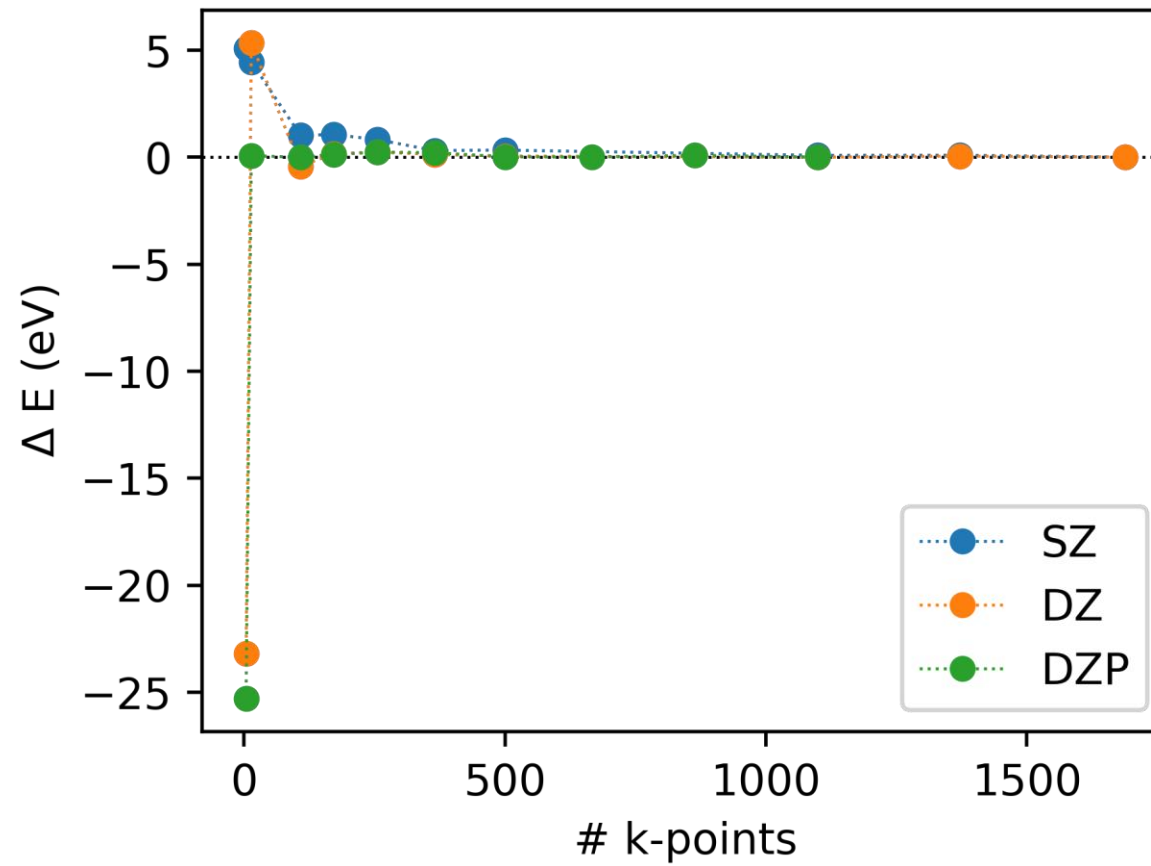


Results for silicon (Si)



Gamma-point calculation with interaction between periodic images Some features might not work optimally

# Metallic systems



Results for gold (Au)

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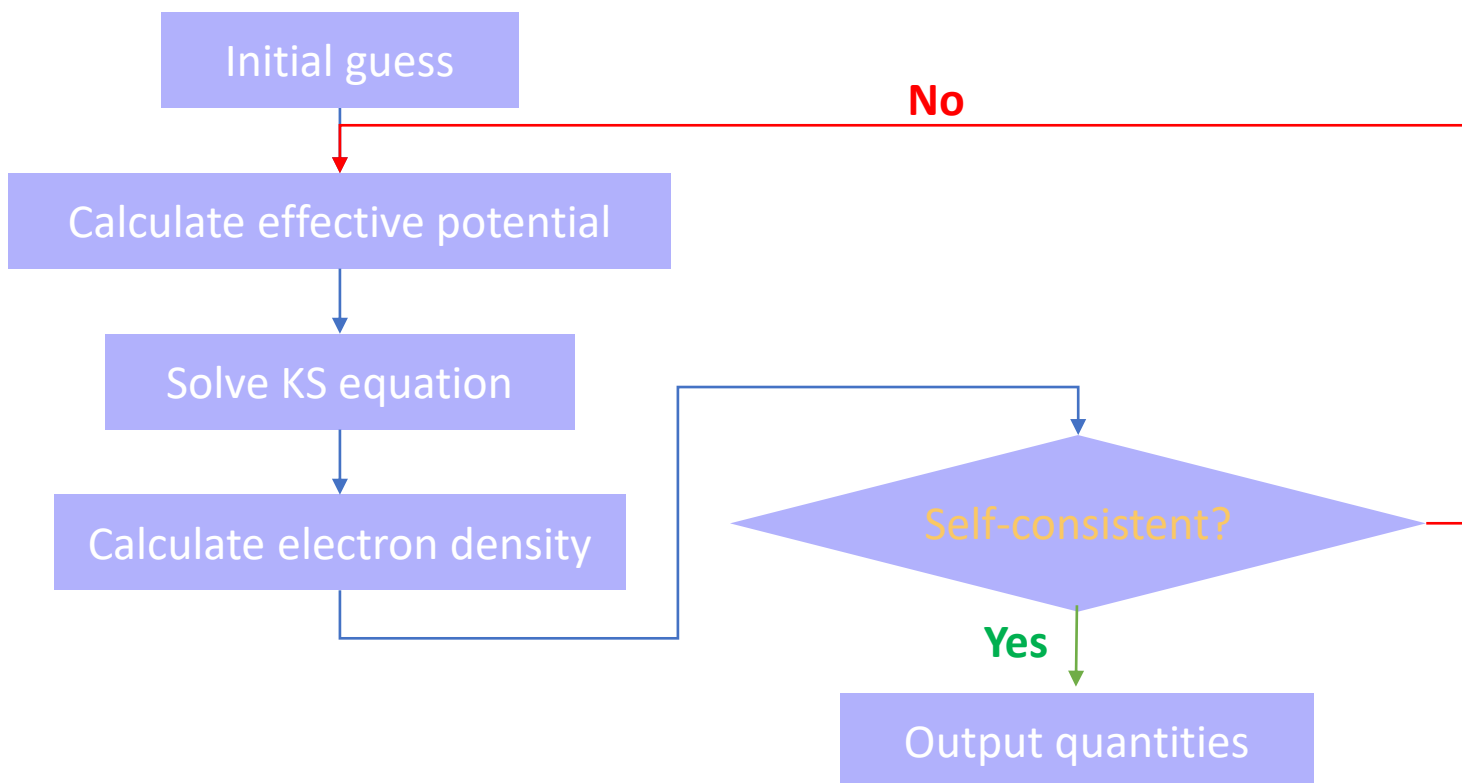
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**day3-wed/04b-KpointConvergence**



SCF convergence

# SCF convergence



- The physical quantity that is mixed:
  - Density matrix
  - Hamiltonian matrix
- Mixing algorithm:
  - Linear
  - Broyden
  - Pulay } N previous steps

# SCF convergence

- SCF.Mix [default Hamiltonian]:
  - Density -> for systems hard to converge
  - Hamiltonian
- SCF.MixerMethod [default Pulay]
  - Linear
  - Pulay
  - Broyden
- SCF.Mixer.Weight [default 0.25]
  - 0.001 systems hard to converge ->a lot of steps
  - 0.4 systems easy to converge -> reduce steps
- SCF.Mixer.History [default 2]
- Max.SCF.Iterations [default 1000]
- SCF.DM.Converge F [default T]
- SCF.H.Converge F [default T]

All of them strongly dependent on the system!!

```
SCF.Mix Hamiltonian
```

```
SCF.MixerMethod Pulay
```

```
SCF.Mixer.Weight 0.3
```

```
SCF.DM.Tolerance 10^-4
```

```
SCF.MaxIterations 1000
```

```
Max.SCF.Iterations 75
```

```
SCF.MixerMethod pulay
```

```
SCF.Mixer.Weight 0.2
```

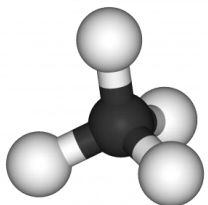
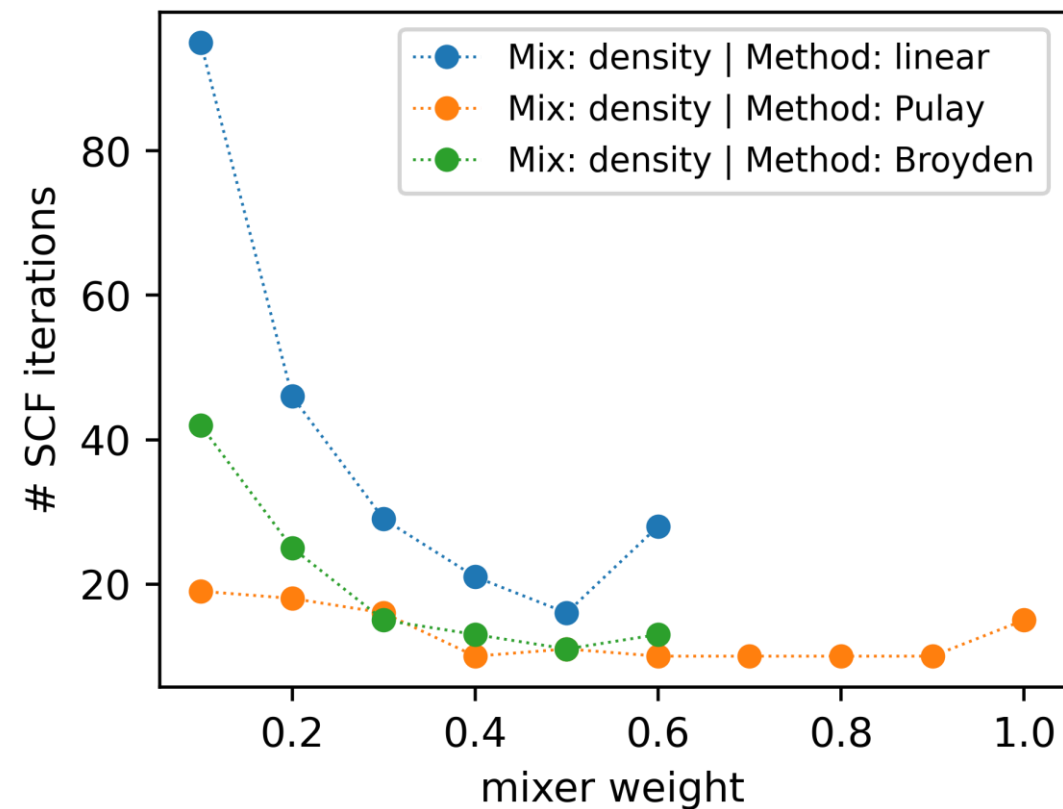
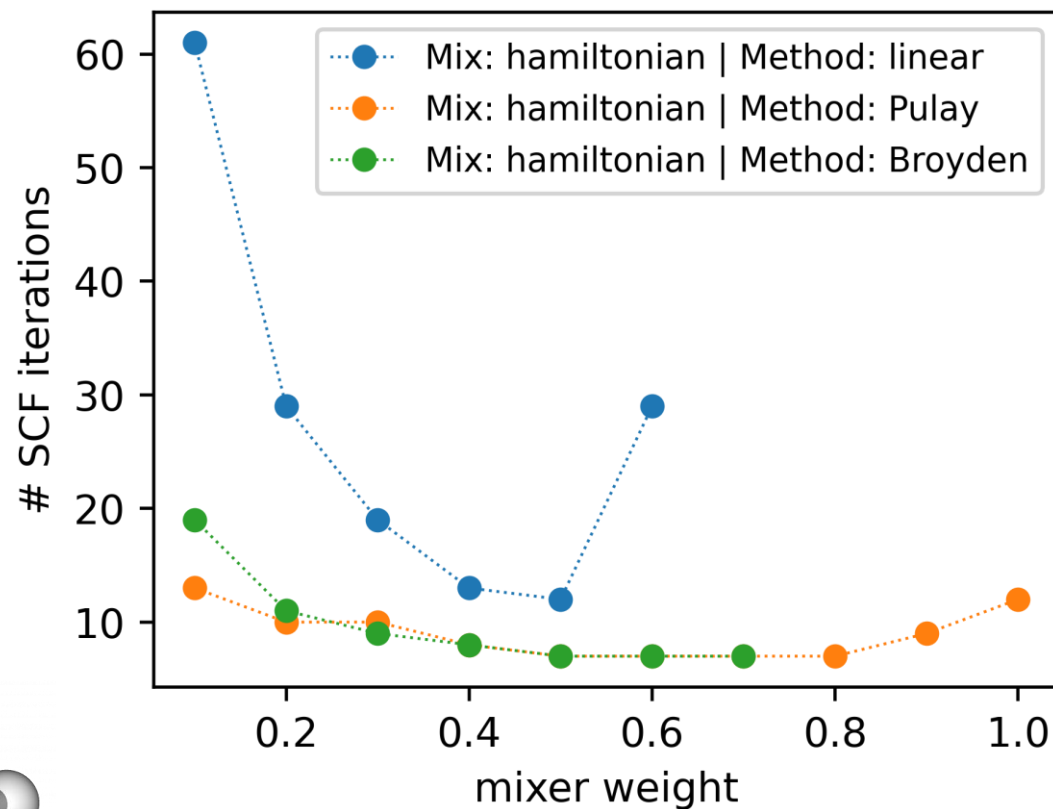
```
SCF.Mixer.History 5
```

More advanced options ... (manual)

# SCF convergence

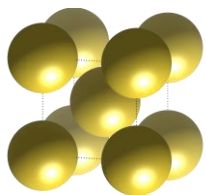
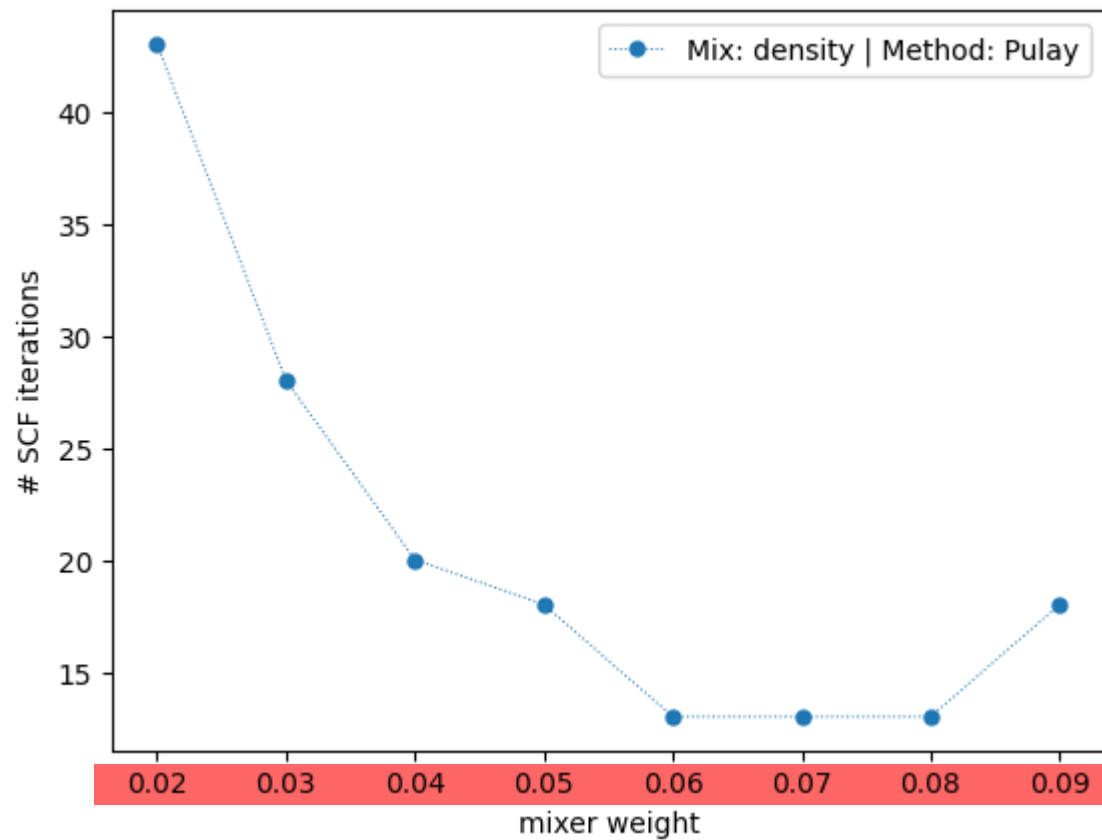
SCF cycle converged

SCF\_NOT\_CONV:



Results for methane (CH4)

# Systems hard to converge



Results for sodium (Na)

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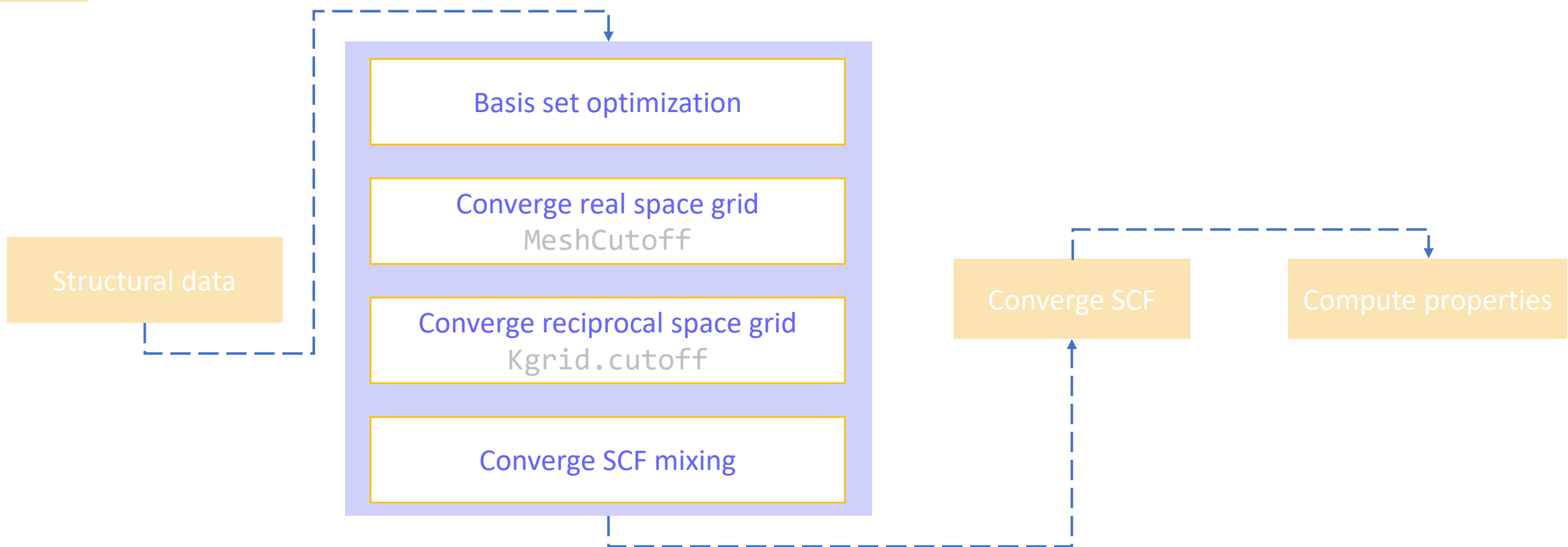
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**day3-wed/04c-SCF**

# How do I converge the whole calculation?





Thank you for your attention

